

# Probing the Early Universe with Galaxy Clustering

Fabian Schmidt

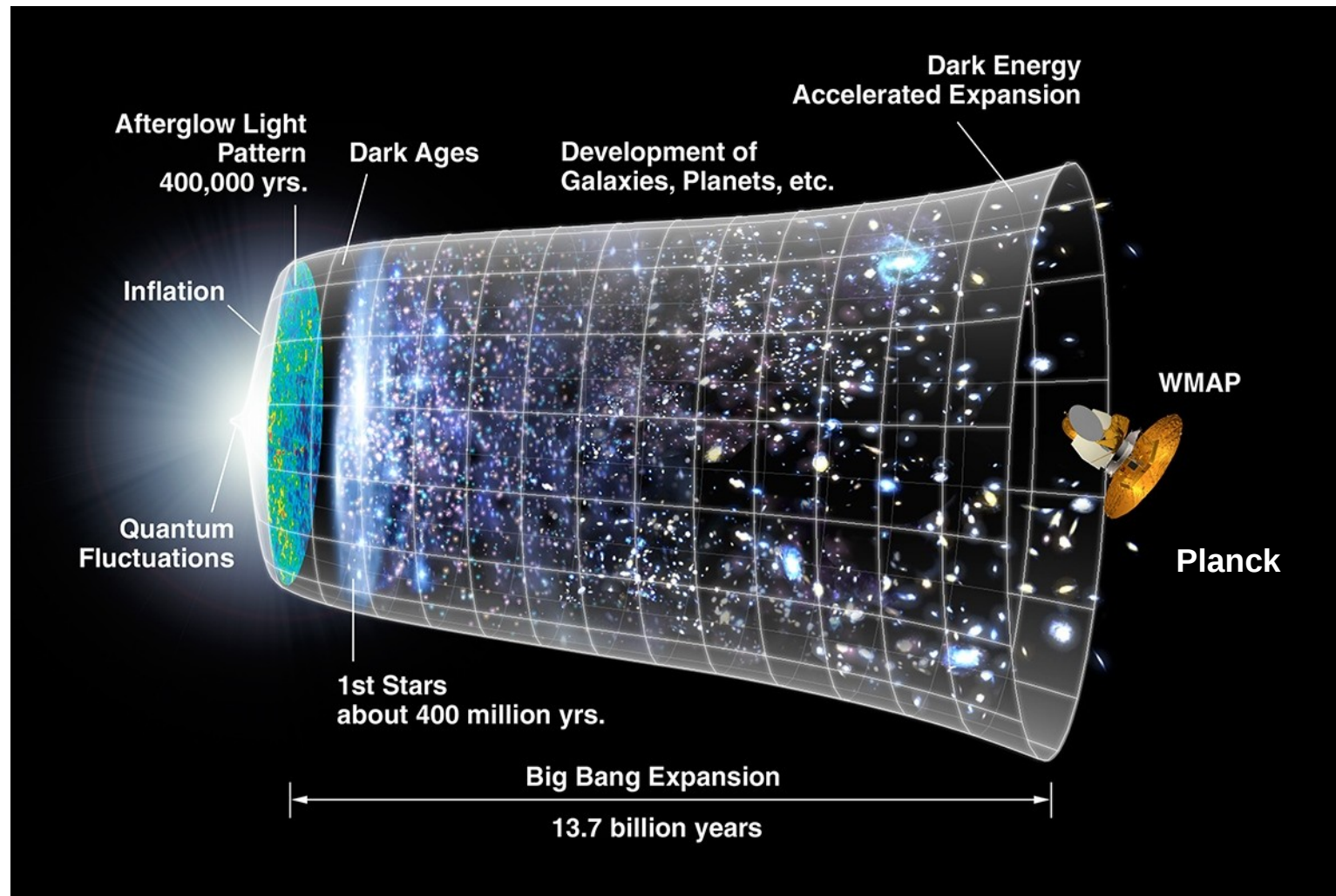
with Francis Cyr-Racine, Vincent Desjacques,  
Donghui Jeong, Marc Kamionkowski,  
Emiliano Sefusatti



Berkeley TAC Seminar, 12/6/11

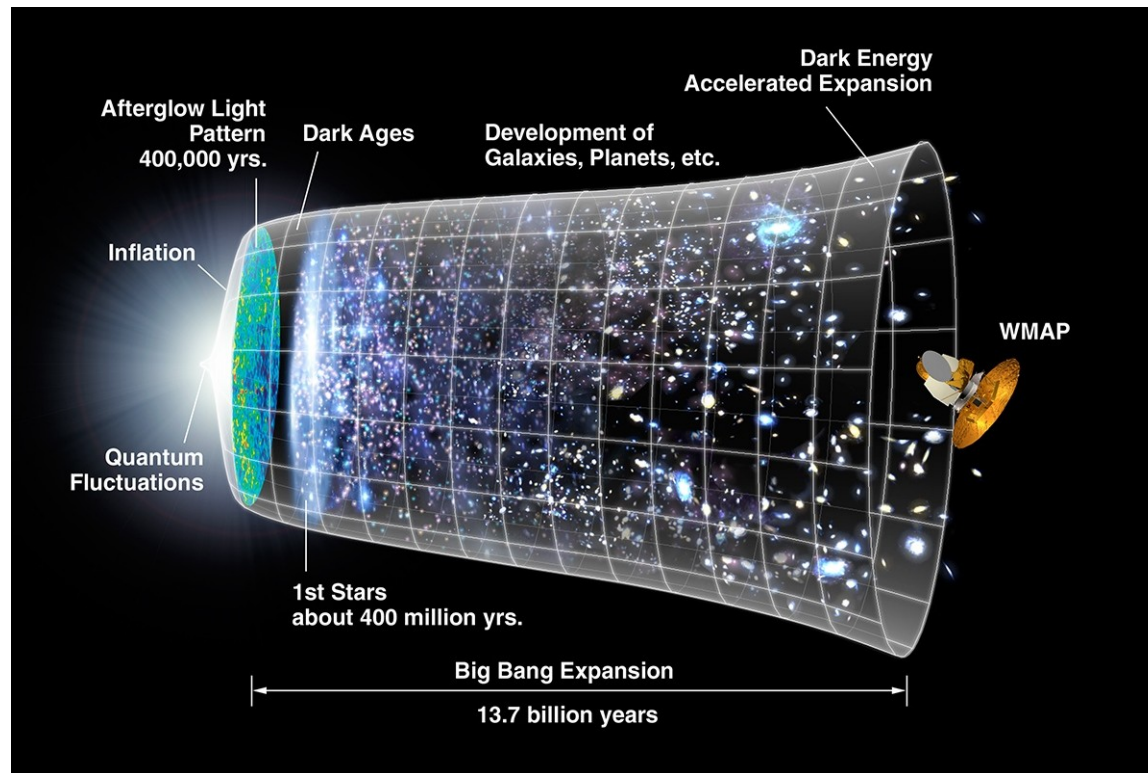
# Introduction

- Pictorial history of the Universe



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- What we would like to know
  - Expansion history  $H(z)$  of background Universe
  - Origin and evolution of perturbations



# Perturbations

- Origin of initial density perturbations in the Universe ?
  - Inflation - most popular scenario
  - Determining physics & energy scale ( $10^3 - 10^{19}$  GeV) of inflation is (one) holy grail of cosmology

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  - CMB -> snapshot at  $z \sim 1100$
  - Subsequent evolution determined by gravity  
--> probe dark matter, *General Relativity*

# Perturbations

- Origin of initial density perturbations in the Universe ?  
*Focus of this talk*
  - Inflation - most popular scenario
  - Determining physics & energy scale ( $10^3 - 10^{19}$  GeV) of inflation is (one) holy grail of cosmology
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--> probe dark matter, *General Relativity*

# Aside: a new approach to weak lensing

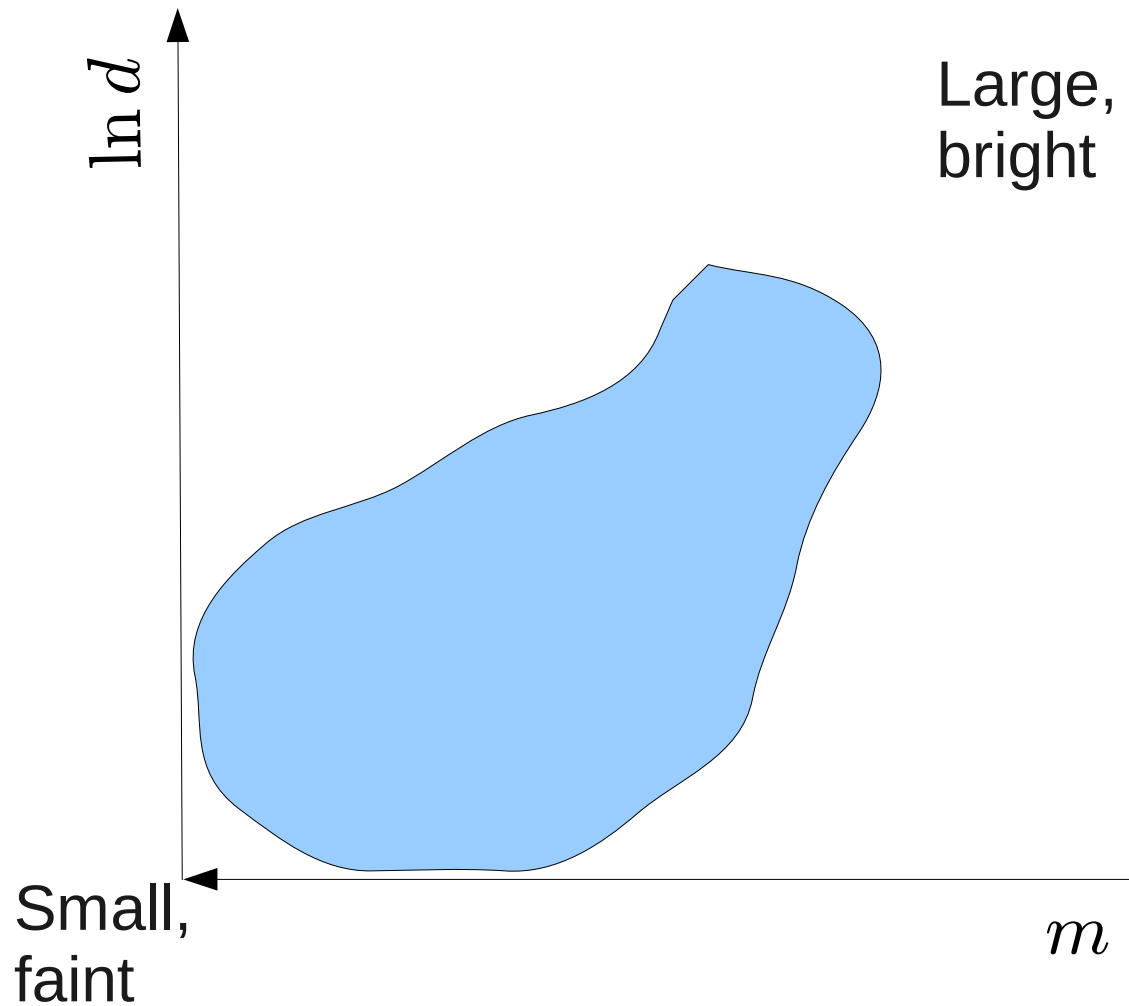
- Standard approach: **shear  $\gamma$** 
  - measured through galaxy shapes
- Idea: measure magnification (**convergence  $\kappa$** )
  - using galaxy fluxes/sizes
- Additional **signal-to-noise / lensing information**
  - $\kappa$  and  $\gamma$  measure *different quantities*:

$$\kappa(\vec{r}) = \Sigma(\vec{r}) / \Sigma_{\text{crit}}$$

$\Sigma$ : projected surface mass density

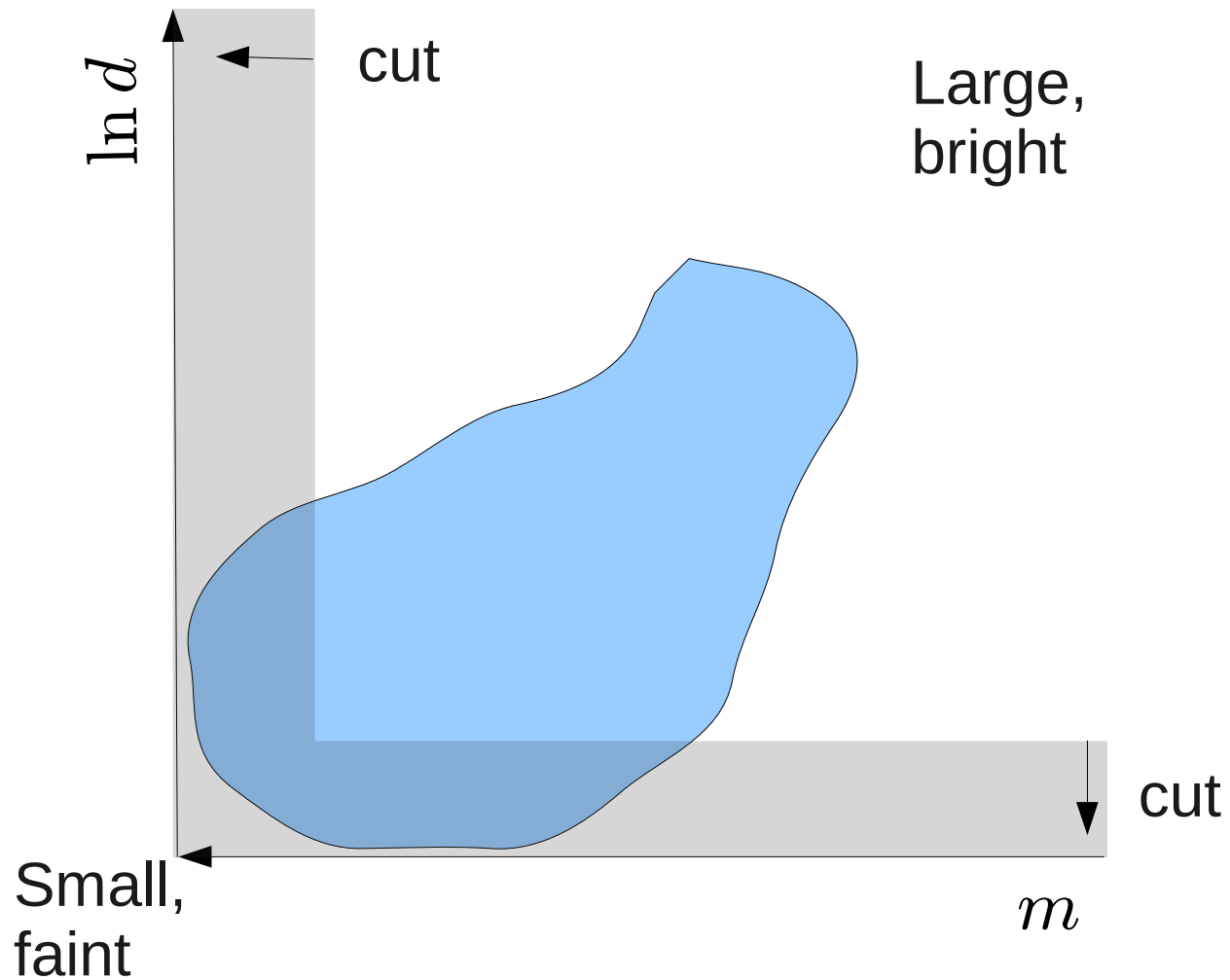
$$\gamma(r) = (\bar{\Sigma}(< r) - \Sigma(r)) / \Sigma_{\text{crit}}$$

# Magnification effect

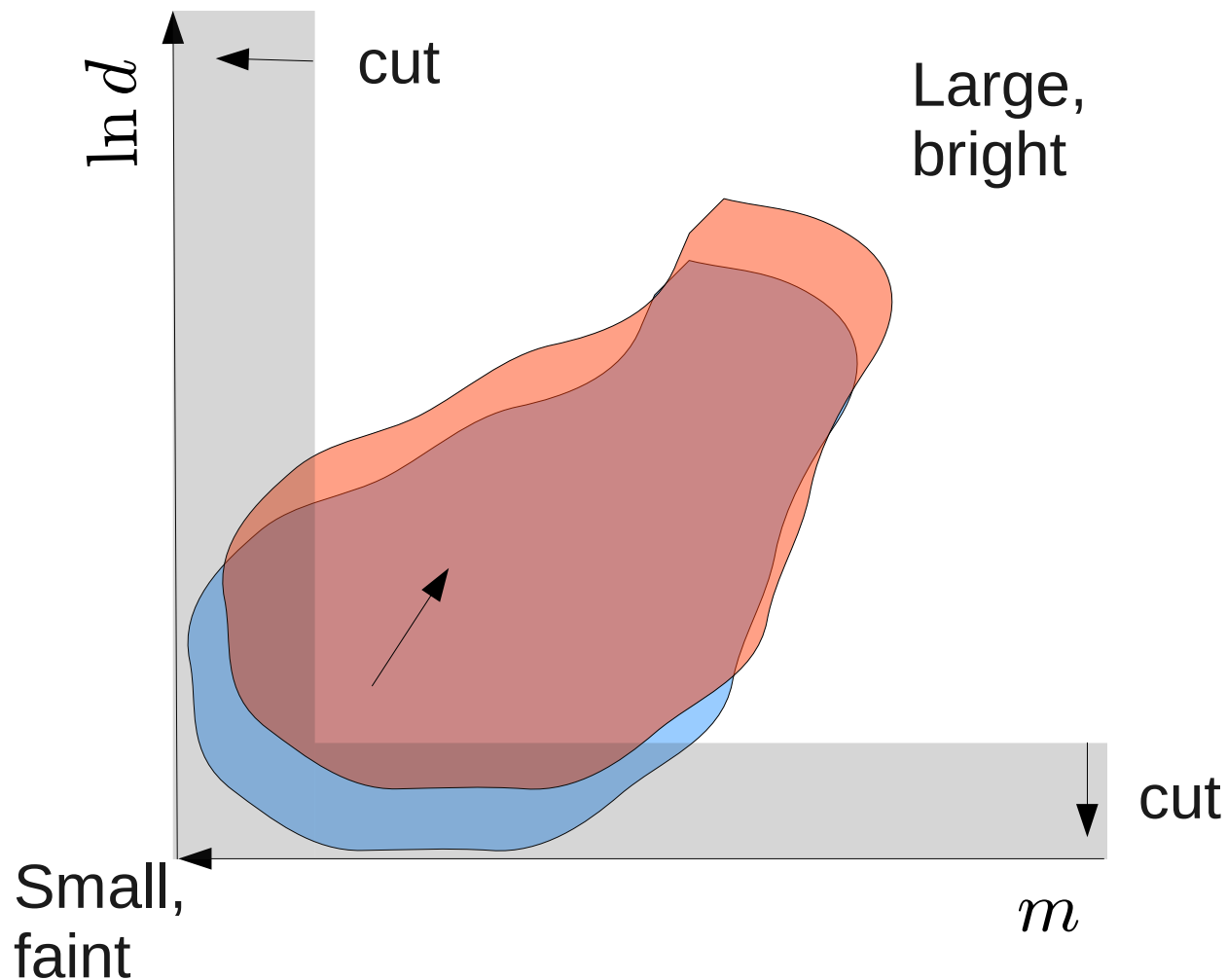




# Magnification effect



# Magnification effect



Sizes:

$$\ln d = \ln d_0 + \eta \kappa$$

Fluxes:

$$m = m_0 + q \kappa$$

$$\eta \approx 1; \quad q \approx -2.1$$

# Estimator for $\Sigma(\kappa)$

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 $m = \text{SExtractor F814w}$*
    - *Both from Hubble ACS data*

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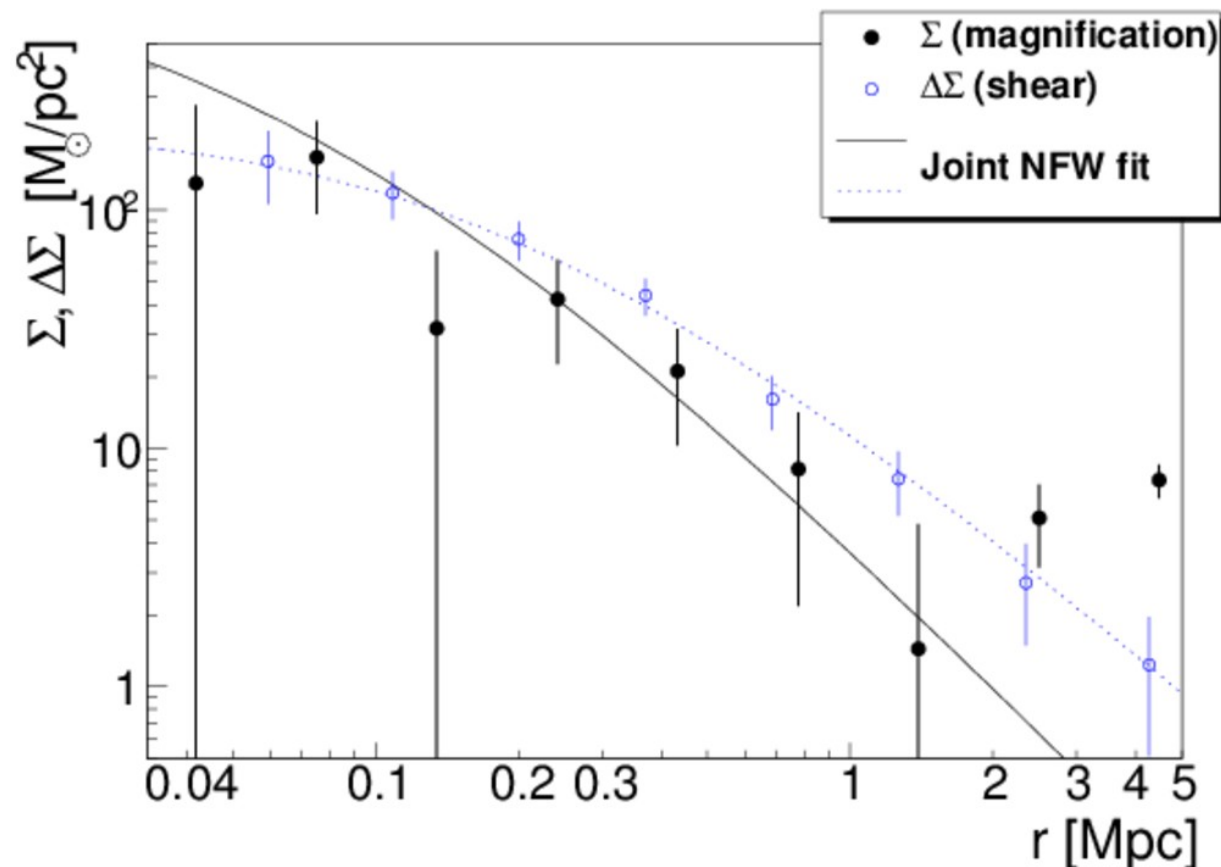
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- Estimator does *not use number density* of sources

# Magnification around X-ray groups in COSMOS

- Stacked group sample  $z=0.2-0.6$



Detection significance:  
~4 $\sigma$  within  $r < 1$  Mpc  
~40% of shear

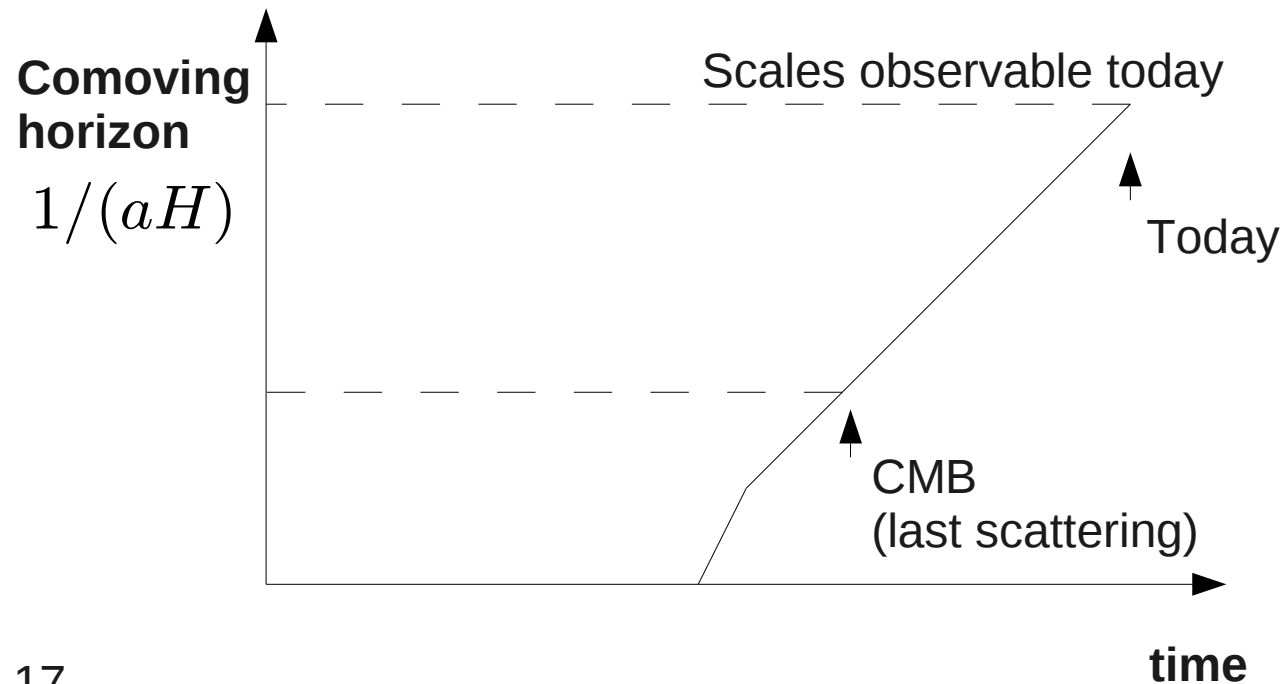
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- Phase of exponential expansion
  - “almost-de Sitter”, driven e.g. by  $V(\phi)$
  - Solves problems of flatness and “superhorizon” correlations



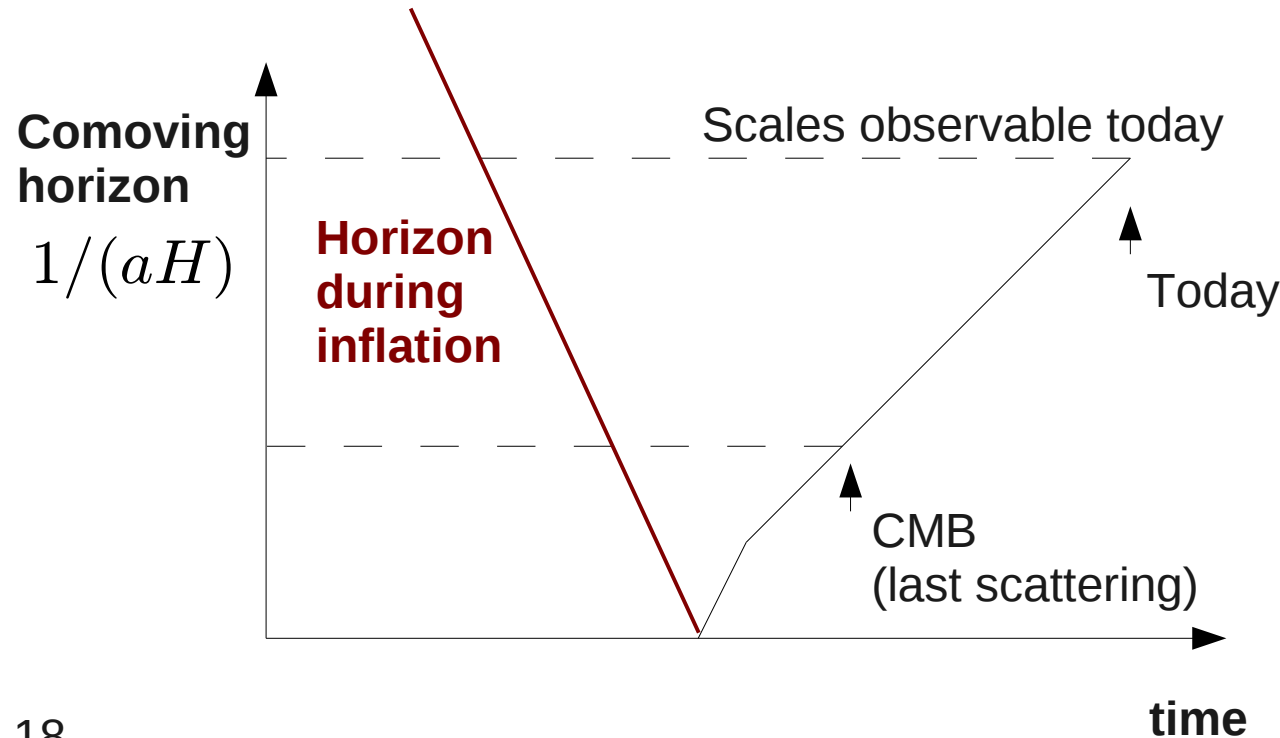
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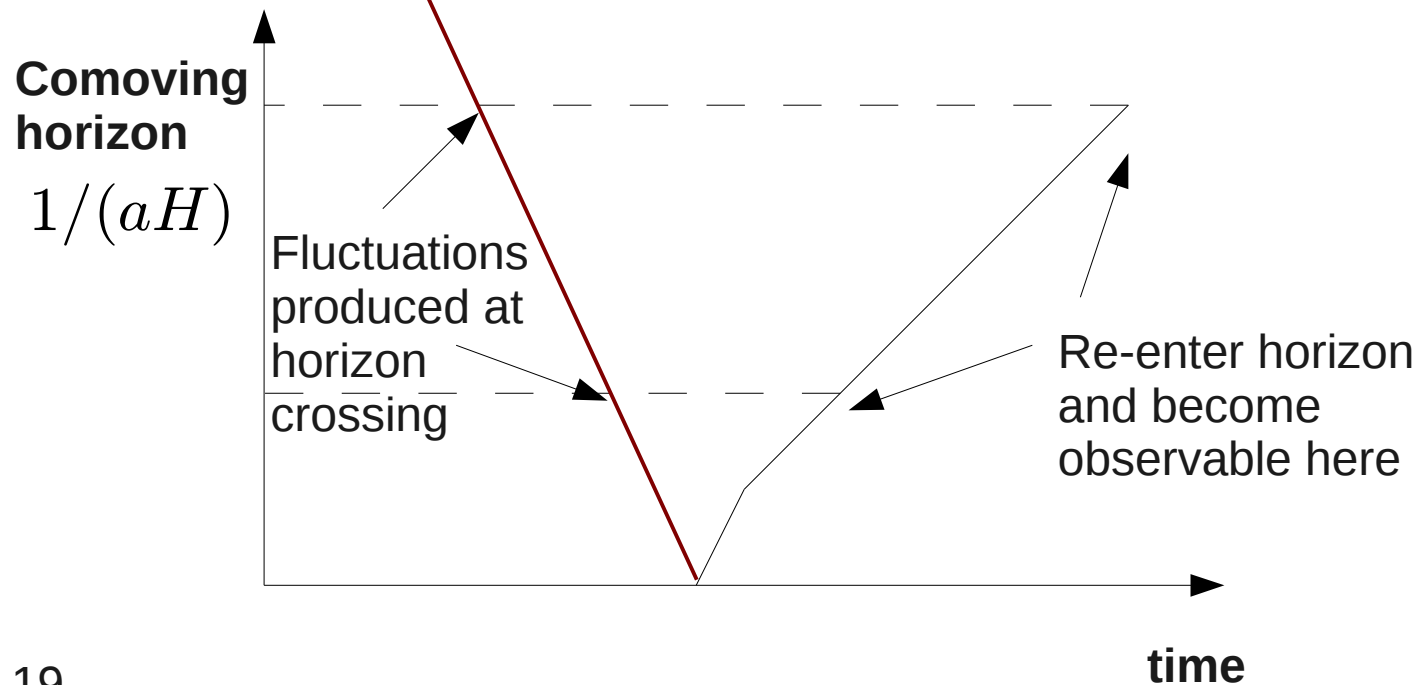
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# Perturbations from Inflation

- Quantum fluctuations “freeze” once outside the horizon
  - Analogous to Hawking radiation
  - We observe them once they re-enter the horizon



# Perturbations from Inflation

- Generic prediction:
  - *almost*-Gaussian fluctuations
  - smooth, *almost* scale-invariant power spectrum (two-point correlation)

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- Generic prediction:
  - *almost*-Gaussian fluctuations
  - smooth, *almost* scale-invariant power spectrum (two-point correlation)
- All information\* on inflation is encoded in *departures* from Gaussianity & scale-invariance
  - So far: one number  $n_s - 1 \approx -0.04 \pm 0.01$

\* in scalar modes. There might be detectable gravitational waves.

# Perturbations from Inflation

- Departures from Gaussianity (= non-Gaussianity) in principle contains much more information
  - Amount and form of NG depends on detailed physics of inflation:
    - Inflaton interactions, sound speed, single-field vs multi-field, initial quantum state, ...

# Perturbations from Inflation

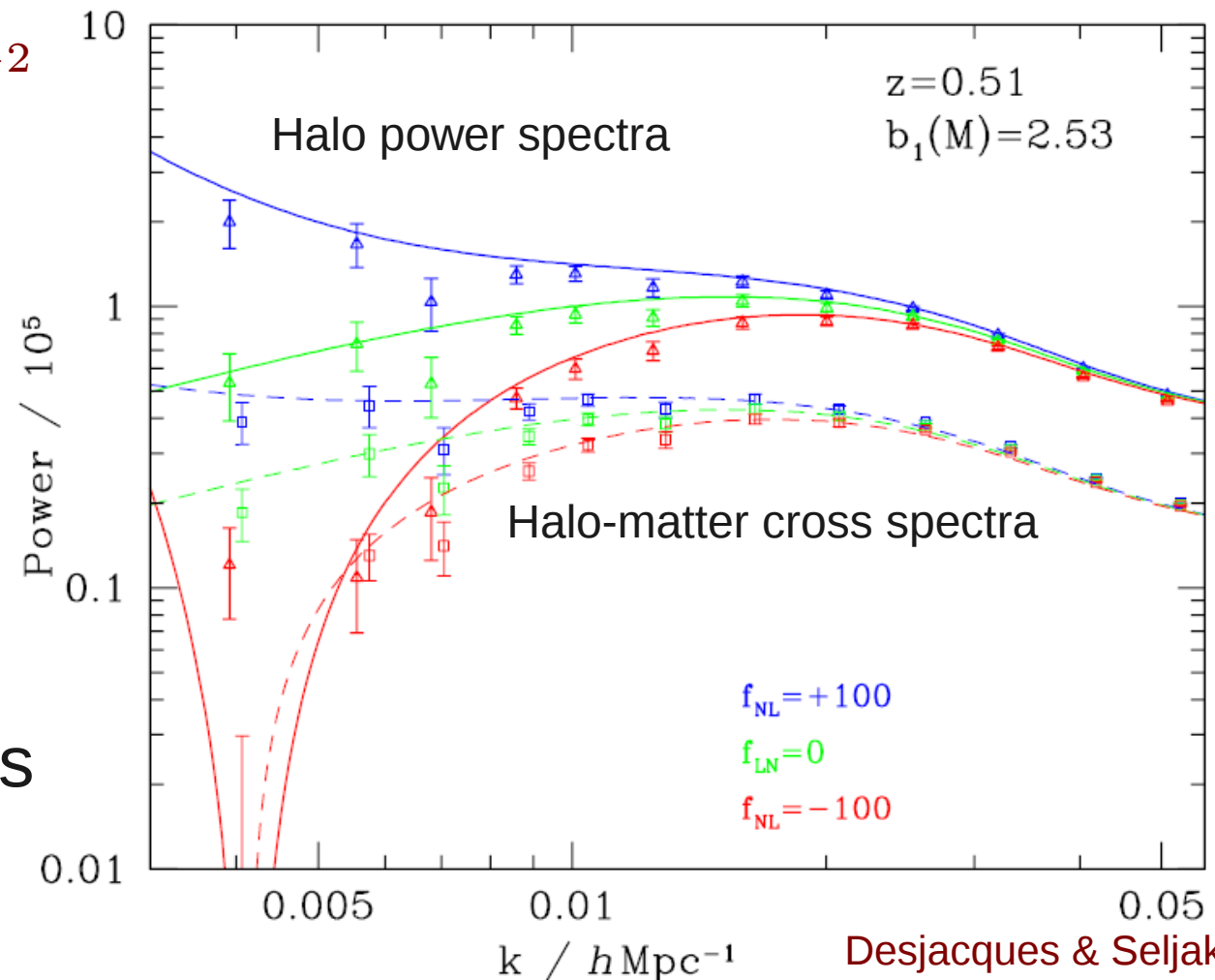
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  - Amount and form of NG depends on detailed physics of inflation:
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- Goal of this talk: describe how we can measure this from galaxy surveys

# Motivation: Halo clustering with *local* NG

- Effect on halo power spectrum from simulations

$$\frac{\Delta P_g(k)}{P_g(k)} = 2 \frac{\Delta b(k)}{b} \propto k^{-2}$$

- Current constraints from SDSS:  
 $|f_{\text{NL}}^{\text{loc}}| \lesssim 90$
- Comparable to CMB constraints





# Statistical description

- A Gaussian field  $\phi$  is completely described by its power spectrum:

$$\langle \phi(\vec{k}) \phi(\vec{k}') \rangle = (2\pi)^3 \delta_D(\vec{k} + \vec{k}') P_\phi(k)$$

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- $\phi = 3\zeta/5$  Bardeen potential during matter domination = Newtonian potential on large scales

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- In non-Gaussian (NG) case, all higher point correlations non-zero
  - However,  $\phi \sim 10^{-5} \rightarrow$  perturbative expansion

# Describing Non-Gaussianity

- Either via *bispectrum*

$$\langle \hat{\phi}(\vec{k}_1) \hat{\phi}(\vec{k}_2) \hat{\phi}(\vec{k}_3) \rangle = (2\pi)^3 \delta_D(\vec{k}_1 + \vec{k}_2 + \vec{k}_3) B_\phi(k_1, k_2, k_3)$$

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- Or via *field redefinition*

$$\hat{\phi}(\vec{k}) = \phi(\vec{k}) + f_{\text{NL}} \int \frac{d^3 \vec{k}_1}{(2\pi)^3} \omega(\vec{k}_1, \vec{k} - \vec{k}_1) \phi(\vec{k}_1) \phi(\vec{k} - \vec{k}_1)$$

Physical, non-Gaussian field

Gaussian random field

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Amplitude parameter

“Shape”

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- Used for initializing N-body simulations



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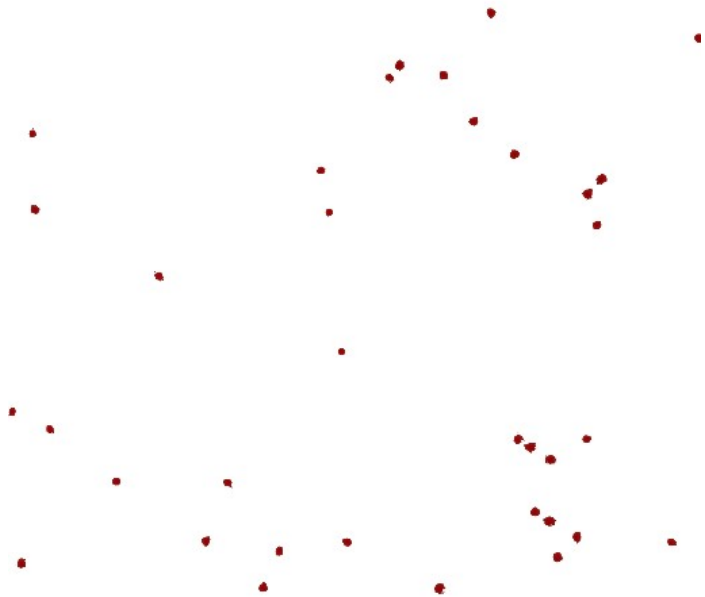
$$\hat{\phi}(\vec{k}) = \phi(\vec{k}) + f_{\text{NL}} \int \frac{d^3 \vec{k}_1}{(2\pi)^3} \omega(\vec{k}_1, \vec{k} - \vec{k}_1) \phi(\vec{k}_1) \phi(\vec{k} - \vec{k}_1)$$

- *Local model:*  $\hat{\phi}(\vec{x}) = \phi(\vec{x}) + f_{\text{NL}} \phi^2(\vec{x})$

$$\Leftrightarrow \omega(\vec{k}_1, \vec{k}_2) = 1$$

# Large Scale Structure

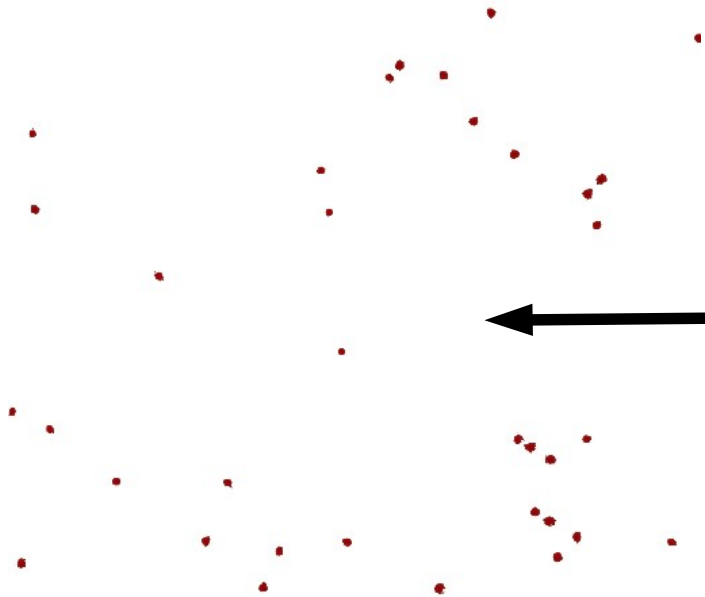
We observe this



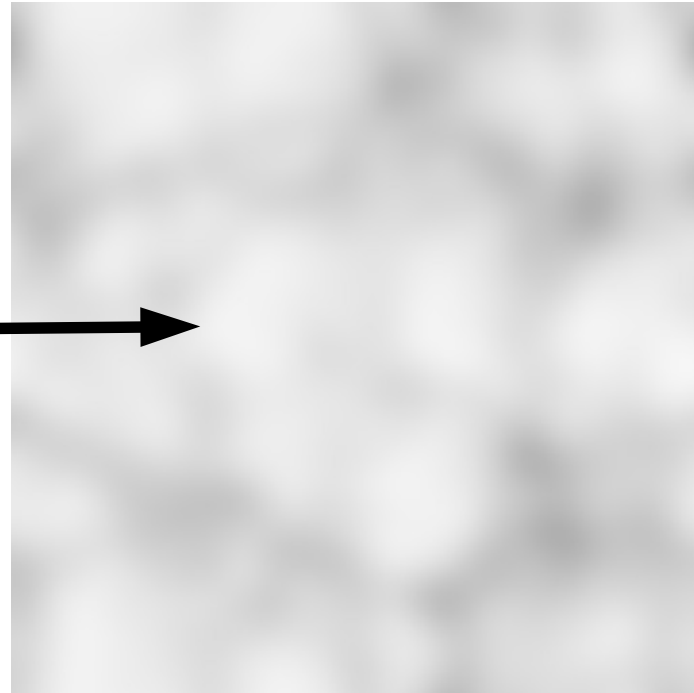
*(dramatization)*

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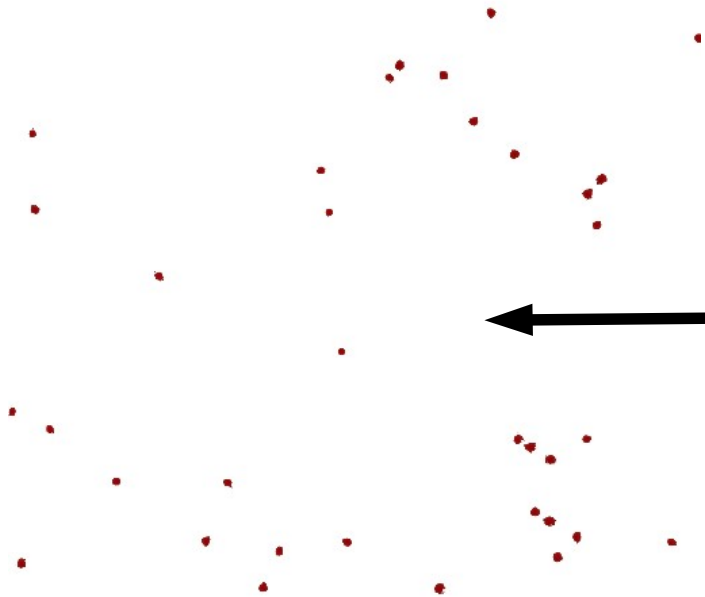
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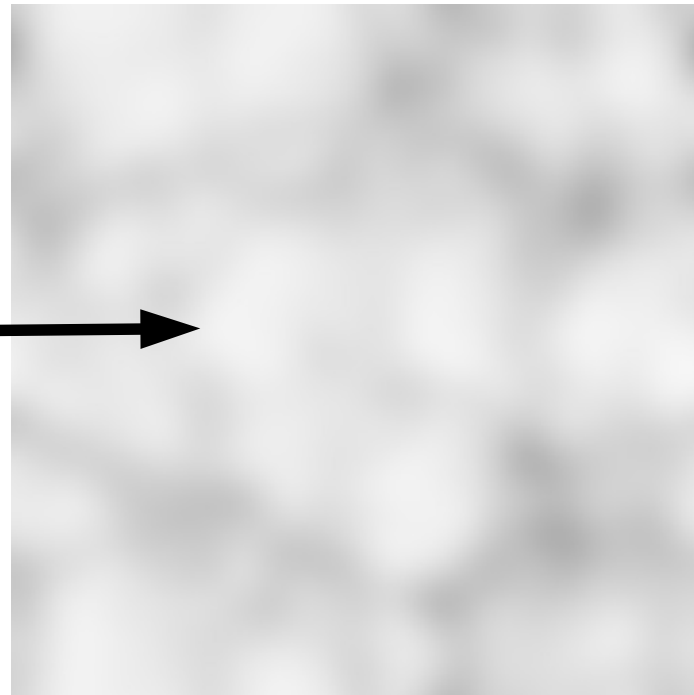
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(dramatization)

- Key theoretical problem:
  - how to map *initial linear fluctuations* to observed *non-linear density field* of tracers (on large scales)

# Large Scale Structure

- We need to map
  - *linear matter overdensity*  $\delta = \frac{\delta\rho_m}{\bar{\rho}_m}$
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  - *linear matter overdensity*  $\delta = \frac{\delta\rho_m}{\bar{\rho}_m}$
  - to *galaxy overdensity*  $\delta_g$
- In the following, focus on *halos*:
  - collapsed, virialized dark matter structures
  - Easy comparison with N-body simulations

# Peak-Background Split (PBS)

(initial, linear)

- Write <sup>✓</sup>perturbations\* as:  $\delta = \delta_l + \delta_s$ ,  $\phi = \phi_l + \phi_s$ , ...

\*Work in synchronous gauge

# Peak-Background Split (PBS)

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“s”: scales which govern halo formation

“l”: scales on which clustering is measured

\*Work in synchronous gauge



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- Definition of bias:  $b_1 = \frac{\partial \ln n_h}{\partial \delta_l} - 1$  Lagrangian bias

$n_h$ : halo number density per  $\ln M$

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corrections relevant  
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- Halo power spectrum:  $P_h(k) = b_1^2 P(k) + \dots$   
corrections relevant on small scales
- $n_h$  depends on  $\rho_{m,l}$  and matter power spectrum
  - Simplest case: through variance on mass scale  $M$ ,  $\sigma_M^2$
  - assume universal mass function for explicit expressions

# Halo Bias in PBS

- Large-scale  $\delta$  changes collapse threshold:

$$\delta_c \rightarrow \delta_c - \delta_l \quad \Rightarrow \quad b_1 = -\frac{\partial \ln n_h}{\partial \delta_c}$$

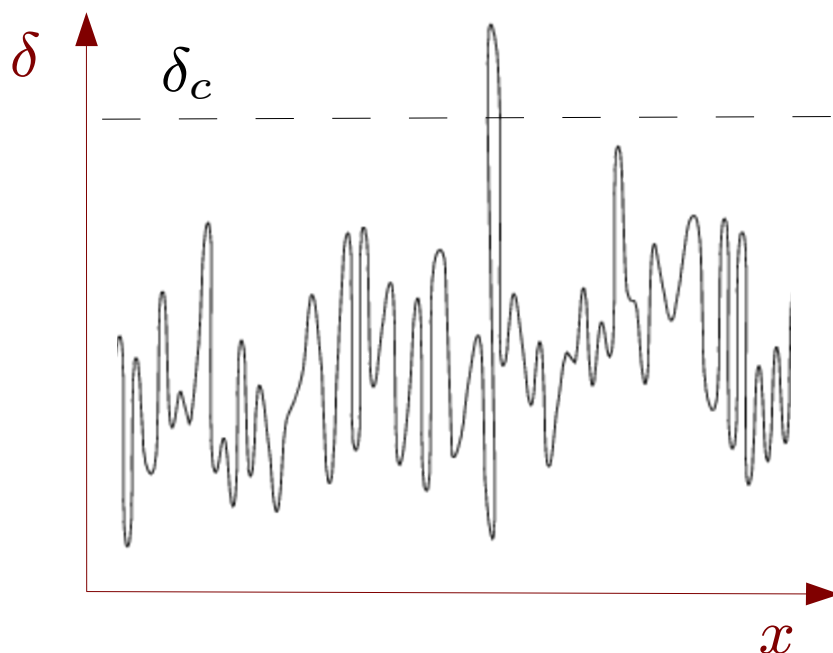
Mo & White 96

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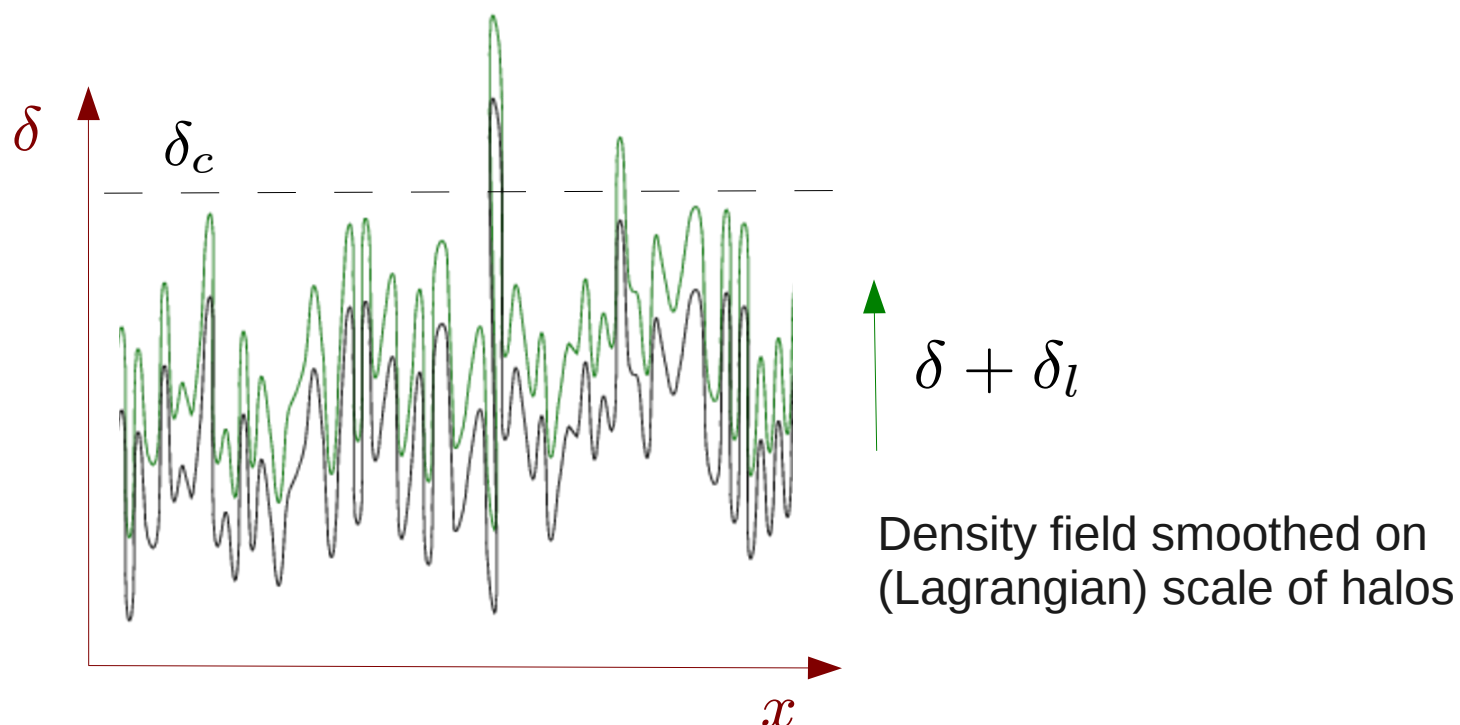
Density field smoothed on  
(Lagrangian) scale of halos

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# Non-Gaussianity and PBS

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- Small-scale density field is rescaled by (long-wavelength) potential perturbations

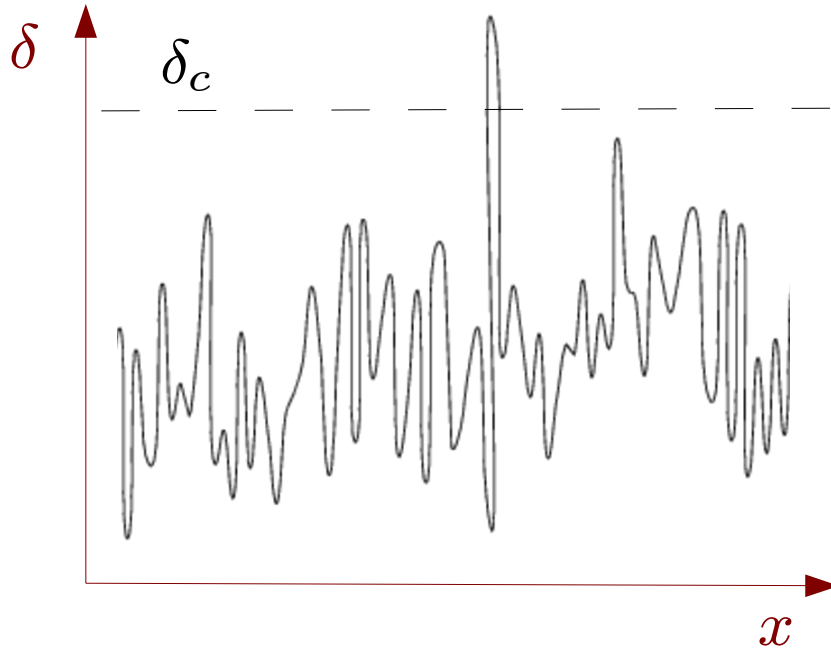
- Variance on mass scale M:

$$\hat{\sigma}_M^2(\vec{x}) = \sigma_M^2[1 + 4f_{\text{NL}}\phi(\vec{x})]$$

Dalal et al,  
Slosar et al

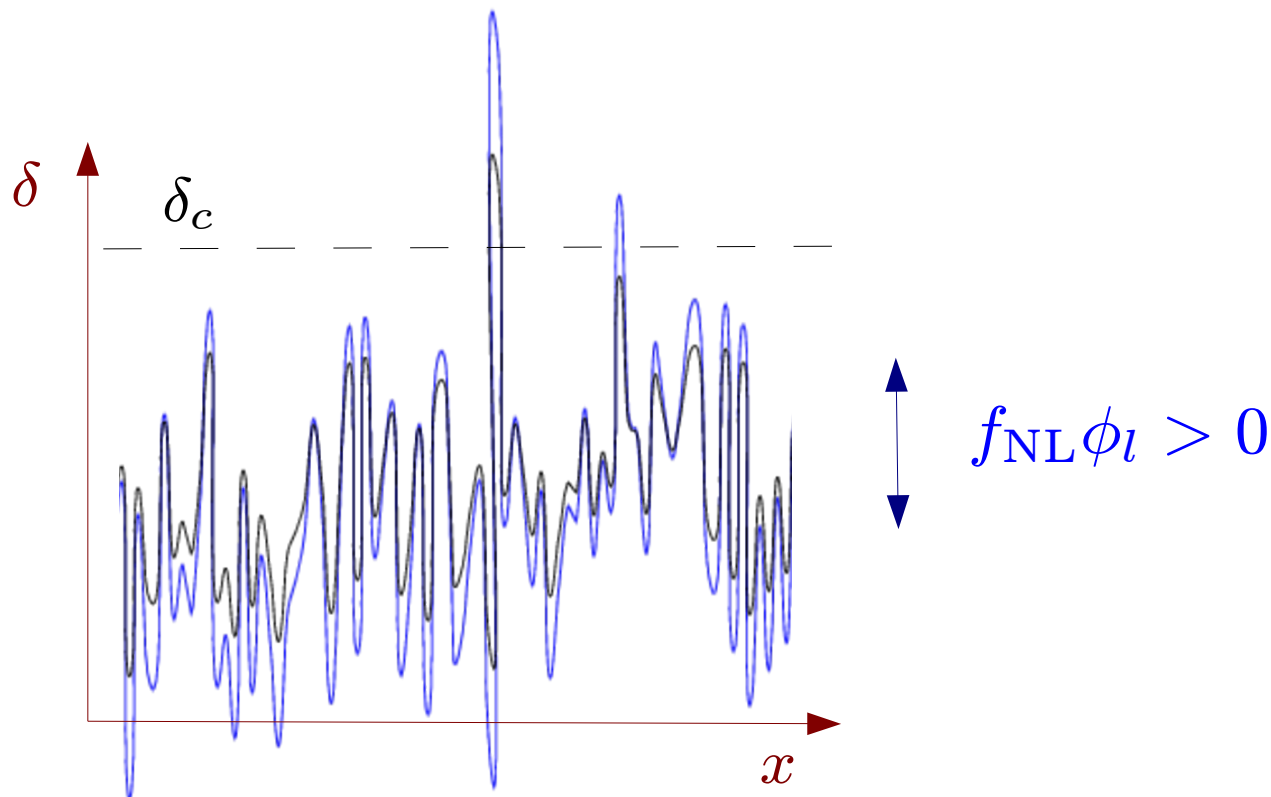
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$$\sigma_{\omega M}^2(k) \equiv \int \frac{d^3 k_s}{(2\pi)^3} \omega(\vec{k}, \vec{k}_s) W_M^2(k_s) P(k_s)$$

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- Note: coupling of potential with density in general depends on  $k$  and  $M$

# Non-Gaussian halo bias

- Just a matter of chain rule...
  - In standard formalism,  $n_h = n_h(\rho_m, \sigma_M)$ ,

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Univ. mass function  
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$\nwarrow$  Univ. mass function or simulations  
 $\nwarrow$  s.a.  
 $\nwarrow$  Linear perturbation theory =  $\mathcal{M}^{-1}(k)$

$$\mathcal{M}(k) = \frac{2}{3} \frac{k^2 T(k) g(z)}{\Omega_m H_0^2 (1+z)}$$

# Predictions for $\Delta b$

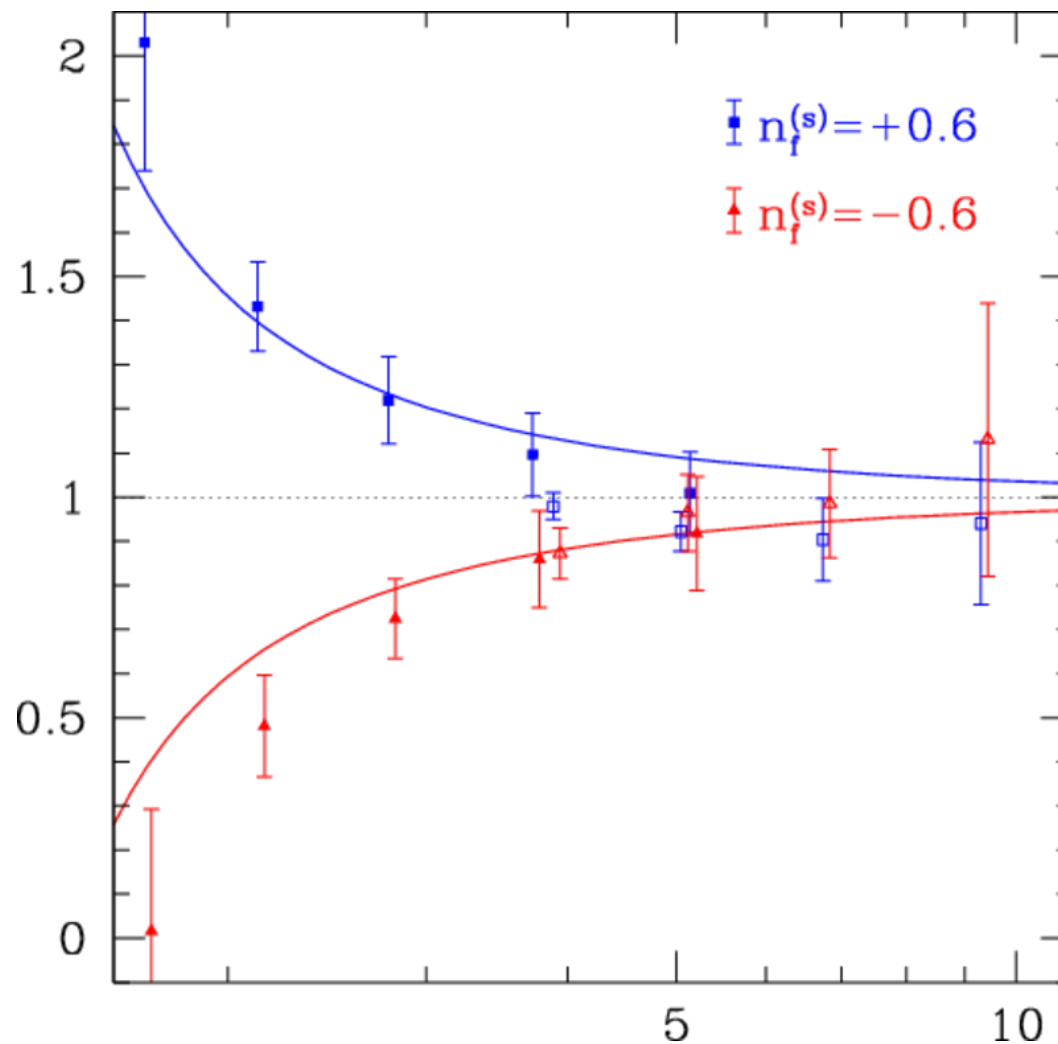
- Scale-invariant bispectra:  $\omega(\vec{k}_s, \vec{k}) = C (k/k_s)^n$
- Examples:
  - *Local model:*  $\omega \rightarrow 1 \Rightarrow \sigma_\omega^2 = \sigma_M^2 \Rightarrow \Delta b_1 \propto k^{-2}$
  - *Equilateral form:*  $\omega \propto k^2 \Rightarrow \Delta b_1 \approx \text{const.}$
  - *Folded form:*  $\omega \propto k \Rightarrow \Delta b_1 \propto k^{-1}$

# Technical detail

- So far, considered effect of NG on  $\nu = \delta_c / \sigma_M$
- Also have to take into account effect on Jacobian  $\frac{d \ln \nu}{d \ln M}$  (since we identify halos by mass, not by  $\nu$ )
- Yields additional term in  $\Delta b$ ,  $\propto \frac{\partial \ln \sigma_{\omega M}^2(k)}{\partial \ln M}$
- Order unity effect for non-local types of NG !

# Updated PBS predictions

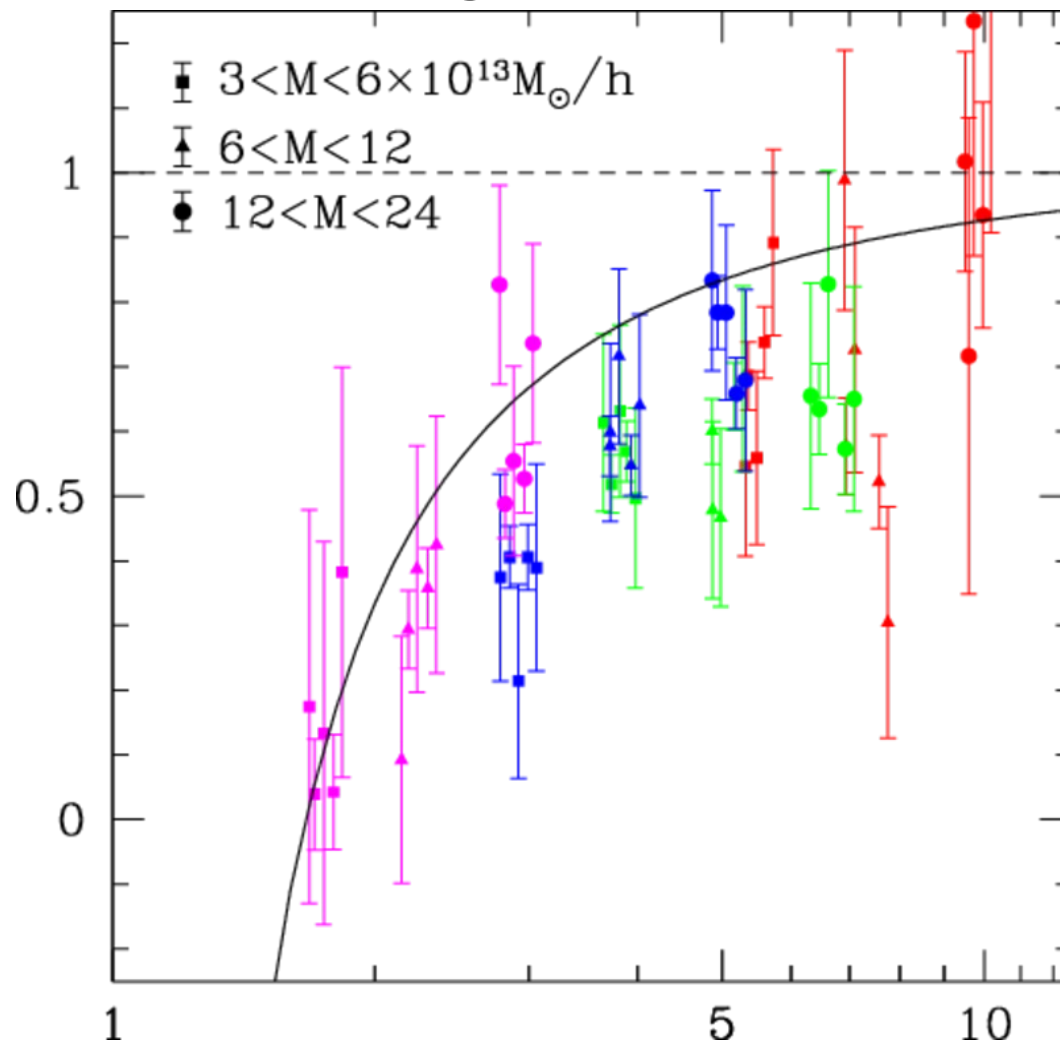
- Scale-dependent local model



Ratio of simulations / new predictions to previous PBS prediction

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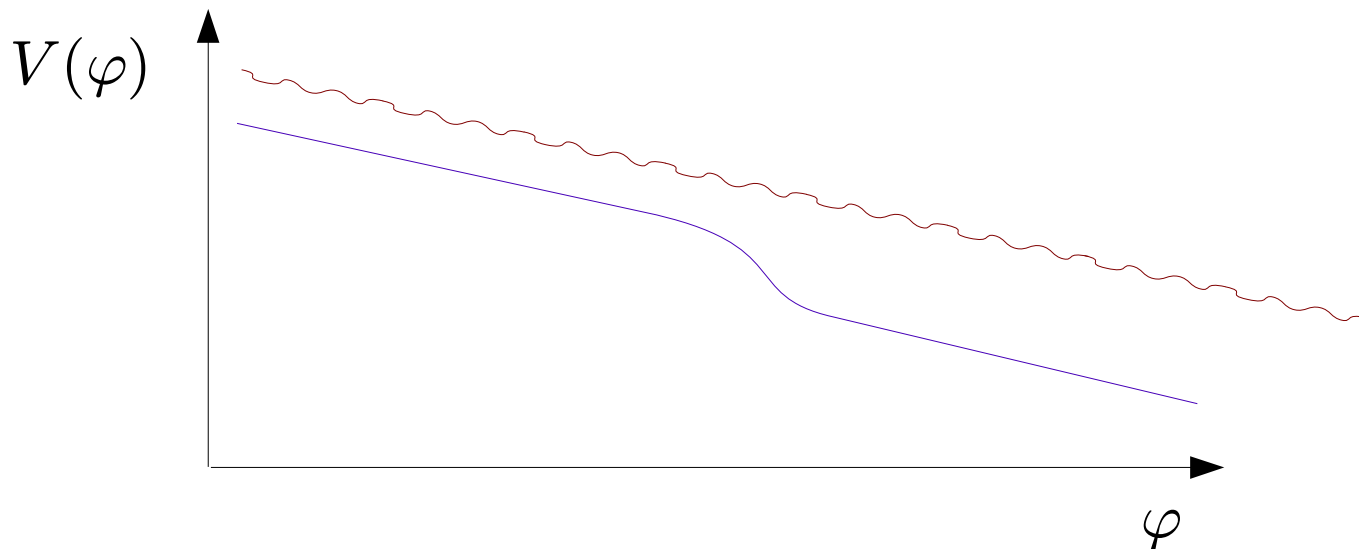
- Folded/orthogonal model



Ratio of simulations / new predictions to previous PBS prediction

# More “interesting” examples...

- Strongly scale-dependent non-Gaussianity
  - Due to **periodic modulation** of, or **feature** in inflaton potential
  - *Violating “slow-roll”*: small effects on  $P(k)$ , but large non-Gaussianity (in standard single-field inflation !)



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- Mode coupling depends strongly on  $k_s$ :

$$\omega(k, k_s) \stackrel{k_s \gg k}{\approx} F(k_s)$$

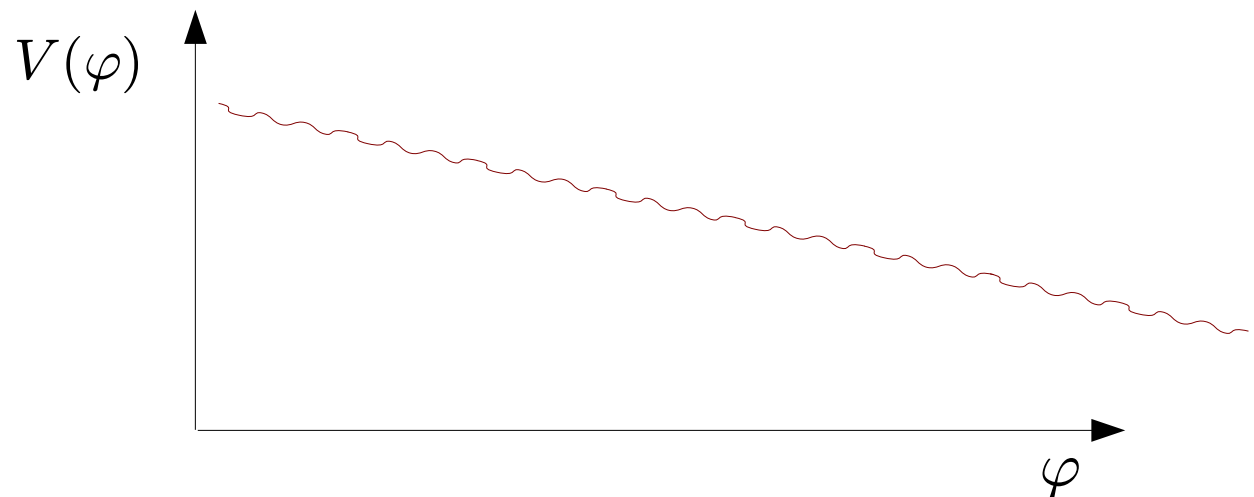
- Scale-dependence as in local model\*:  $\Delta b \propto k^{-2}$

# Resonant Non-Gaussianity

- Periodic modulation of inflaton potential
  - Modes pass through resonance while sub-horizon
  - $\omega(k, k_s) \propto \sin(C_\omega \ln k_s/k_*)$

Flauger & Pajer

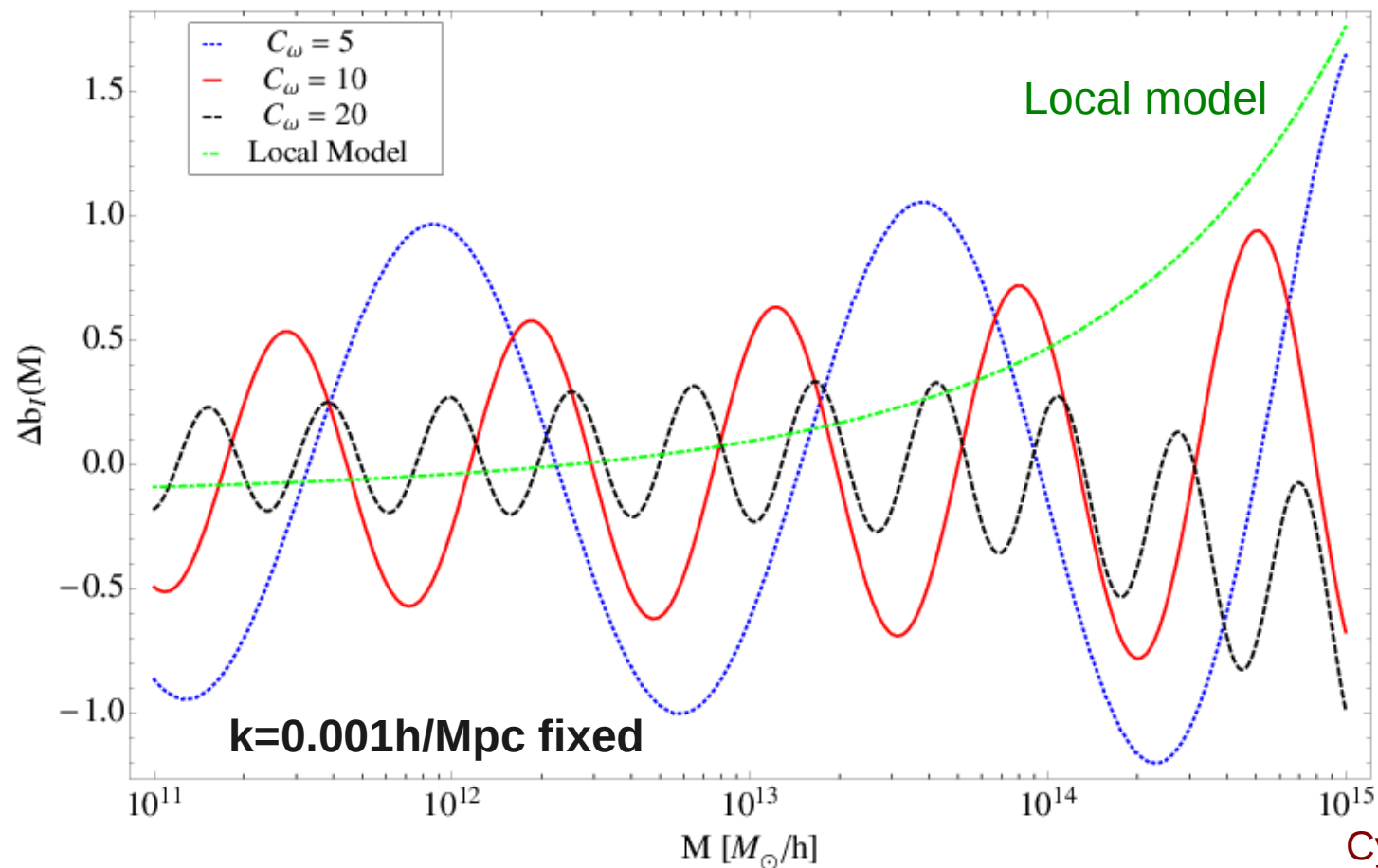
- Consider models that pass current CMB constraints





# Resonant Non-Gaussianity

- $\Delta b$  as function of halo mass
  - Oscillations in *mass-dependence* of galaxy clustering



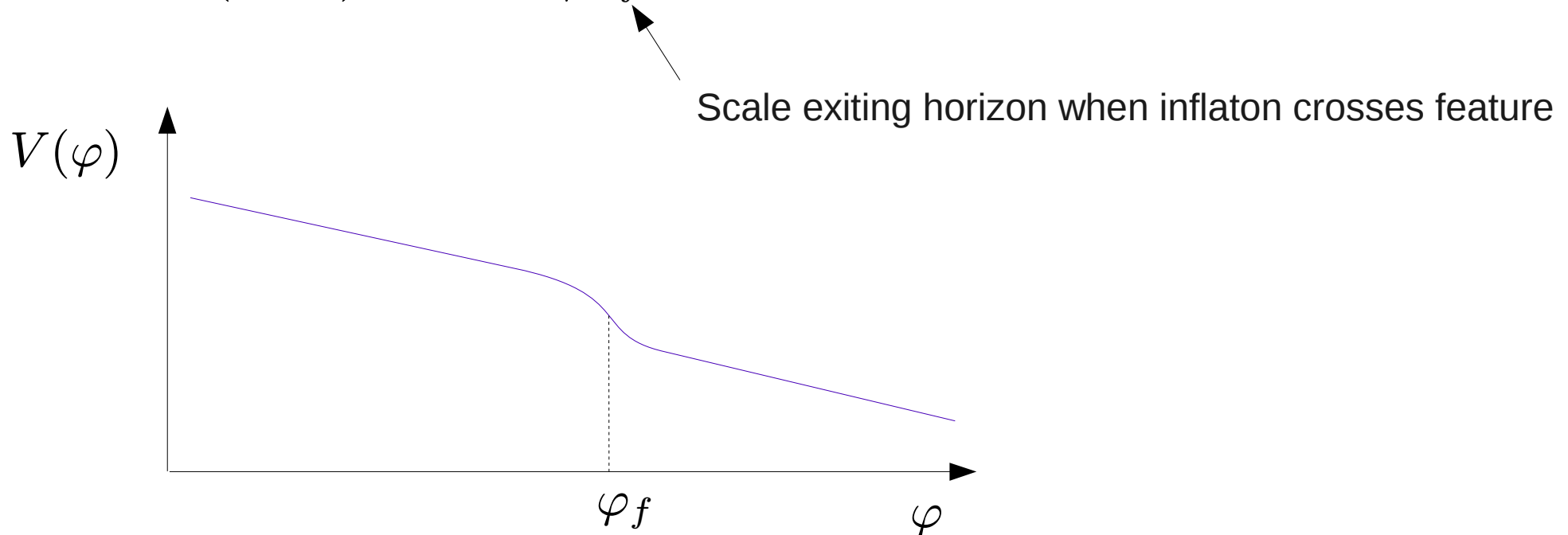
New term  
from Jacobian  
crucial

# Feature in Inflaton Potential

- Bump or step in the potential generates non-Gaussianity

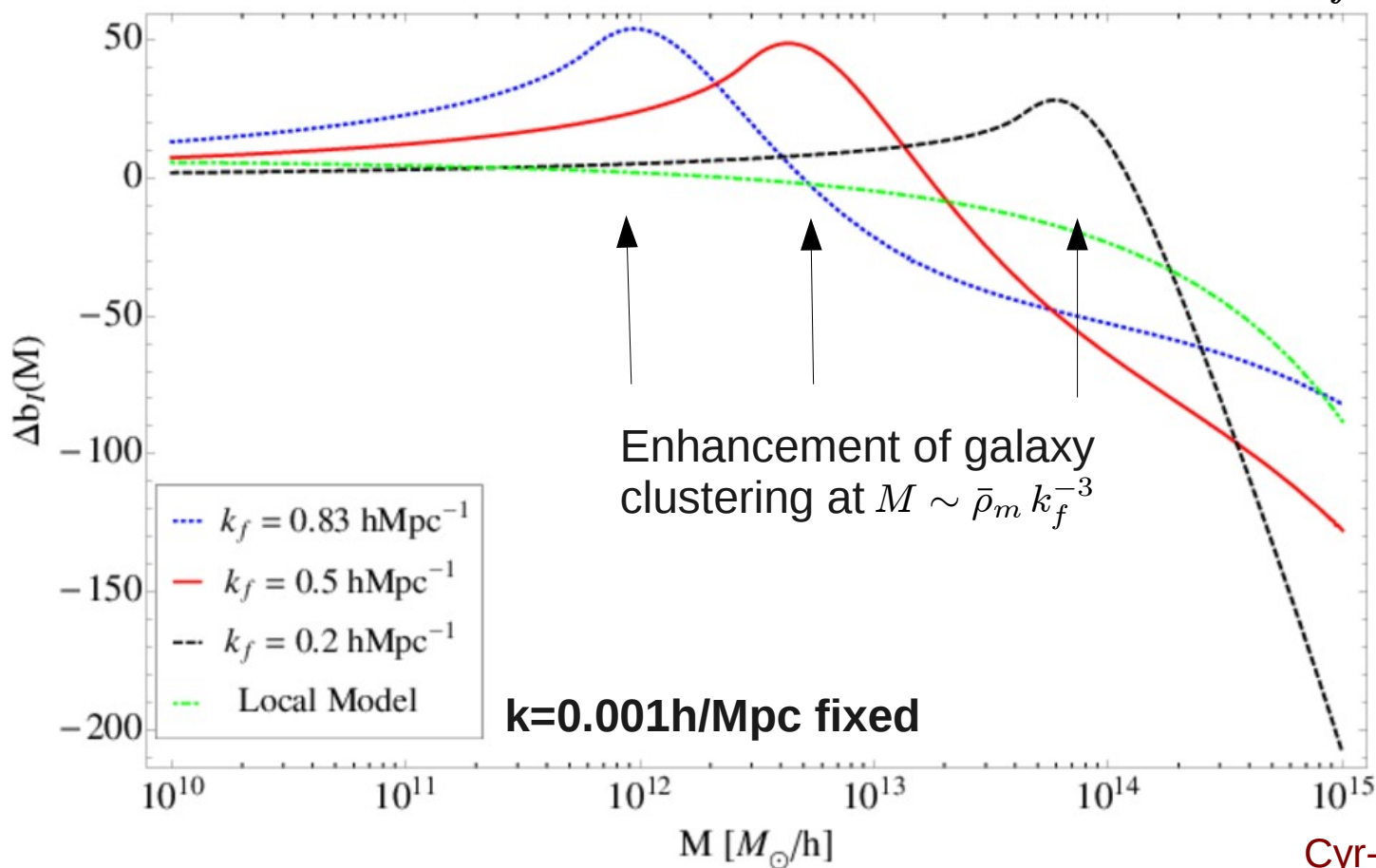
X. Chen et al

- temporarily breaking slow-roll
- $\omega(k, k_s) \propto \sin k_s / k_f$



# Feature in Inflaton Potential

- $\Delta b$  as function of halo mass
  - Feature appears at mass scale  $M \sim \bar{\rho}_m k_f^{-3}$



Constraints on  $k_f$   
complementary to  
CMB

# Galaxy clustering in relativistic context

- Scale-dependent bias  $\propto (k/H)^{-2}$  raises issue of relativistic corrections
- Covariant expression for galaxy density (three-form) simplifies in synchronous gauge
  - Equal time hypersurface = constant-age hypersurface

$$N = \int_{V_{\text{obs}}} \sqrt{-g} n_g(x_{\text{true}}^\alpha) \frac{1}{a(x_{\text{true}}^0)} \left| \frac{\partial x_{\text{true}}^i}{\partial x_{\text{obs}}^j} \right| d^3 x_{\text{obs}}$$

Yoo et al, 2009  
Challinor & Lewis 2011  
Baldauf et al 2011  
Jeong, FS, Hirata 2011

# Galaxy clustering in GR

$$N = \int_{V_{\text{obs}}} \sqrt{-g} n_g(x_{\text{true}}^\alpha) \frac{1}{a(x_{\text{true}}^0)} \left| \frac{\partial x_{\text{true}}^i}{\partial x_{\text{obs}}^j} \right| d^3 x_{\text{obs}}$$

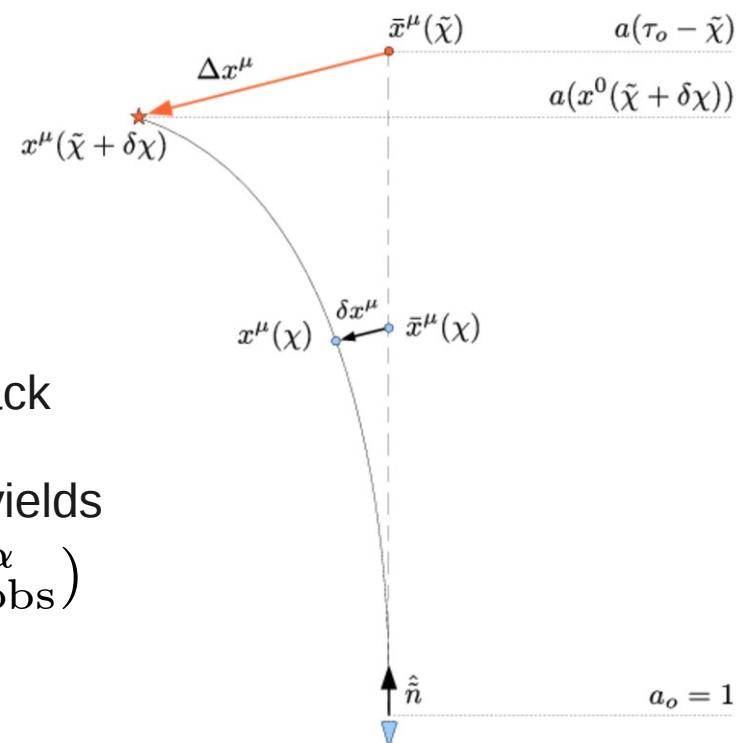
Intrinsic galaxy density

Deflection

Volume distortion

Tracing back  
perturbed  
geodesic yields

$$x_{\text{true}}^\mu(x_{\text{obs}}^\alpha)$$



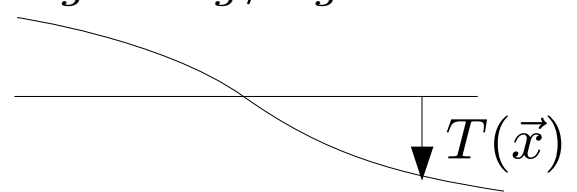
# Galaxy Bias

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$$\tau \rightarrow \tau + T :$$

$$\delta_g = n_g / \bar{n}_g - 1$$


The diagram illustrates the gauge transformation  $T(\vec{x})$ . It shows a horizontal line representing a reference level. A curve, representing the density contrast  $\delta_g$ , crosses this line. A vertical arrow points from the curve down to the horizontal line, labeled  $T(\vec{x})$ , indicating the gauge transformation that shifts the curve to the reference level.

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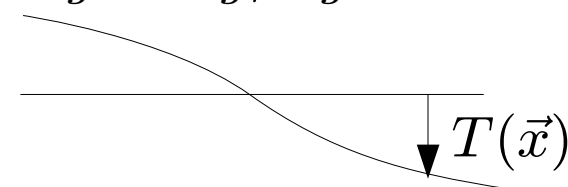
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$$\delta_m \rightarrow \delta_m - 3aHT$$

$$\delta_g \rightarrow \delta_g + b_e aHT, \quad b_e = \frac{\partial \ln \bar{n}_g}{\partial \ln a}$$

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Depends on galaxy sample



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- In *what gauge* is galaxy bias linear ?

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  - Local matter density
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- On large scales, galaxies can know about
  - Local matter density
  - Local age of Universe (linear growth factor)
- Hence,  $\delta_g \propto \delta_m$  on constant-age slices
  - synchronous gauge
  - Gauge-invariant expression for galaxy density perturbation:

$$\delta_g = b(\tau)[\delta_m - 3aH\delta\tau] - b_e(\tau)aH\delta\tau$$

↑  
Perturbation in conf. time  
w.r.t. constant-age slice

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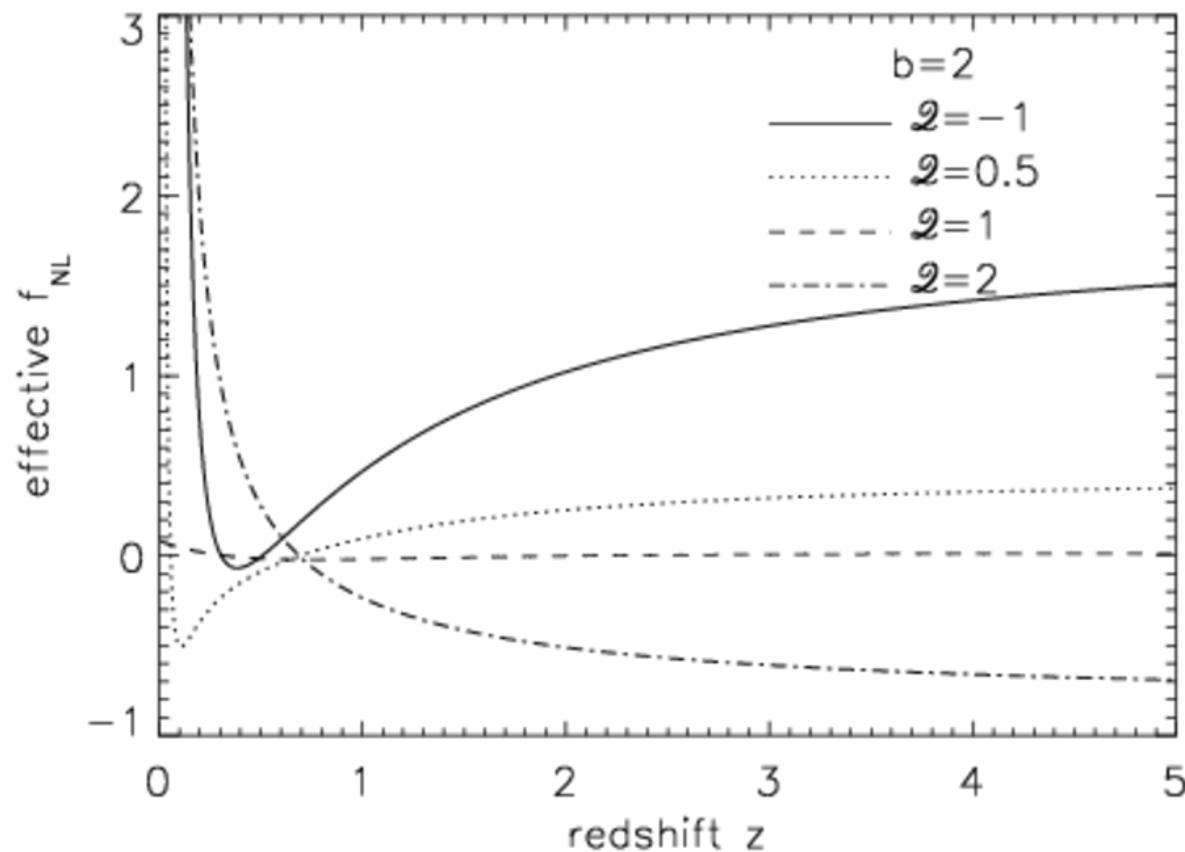
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with  $b(k) = b_1 + 2f_{\text{NL}}(b_1 - 1)\delta_c\mathcal{M}^{-1}(k)$  (for local NG)  
applies in synchronous gauge
- Additional terms from volume distortions, redshift perturbations, ... comparable to effective  $f_{\text{NL,eff}} \lesssim 2$

# NG halo bias in GR context

- Effective  $f_{\text{NL}}$  from GR corrections



$$Q = 5s/2$$

Magn. bias amplitude

# Other ways to look for NG ?

- Why not lensing ?
  - Lots of information in shear maps



# Other ways to look for NG ?

- Why not lensing ?

- Lots of information in shear maps

- Lensing estimators not perfectly linear:

$$\hat{\gamma} = \gamma + b \kappa \gamma + \dots \quad \hat{\kappa} = \kappa + c \kappa^2 + d |\gamma|^2 + \dots$$

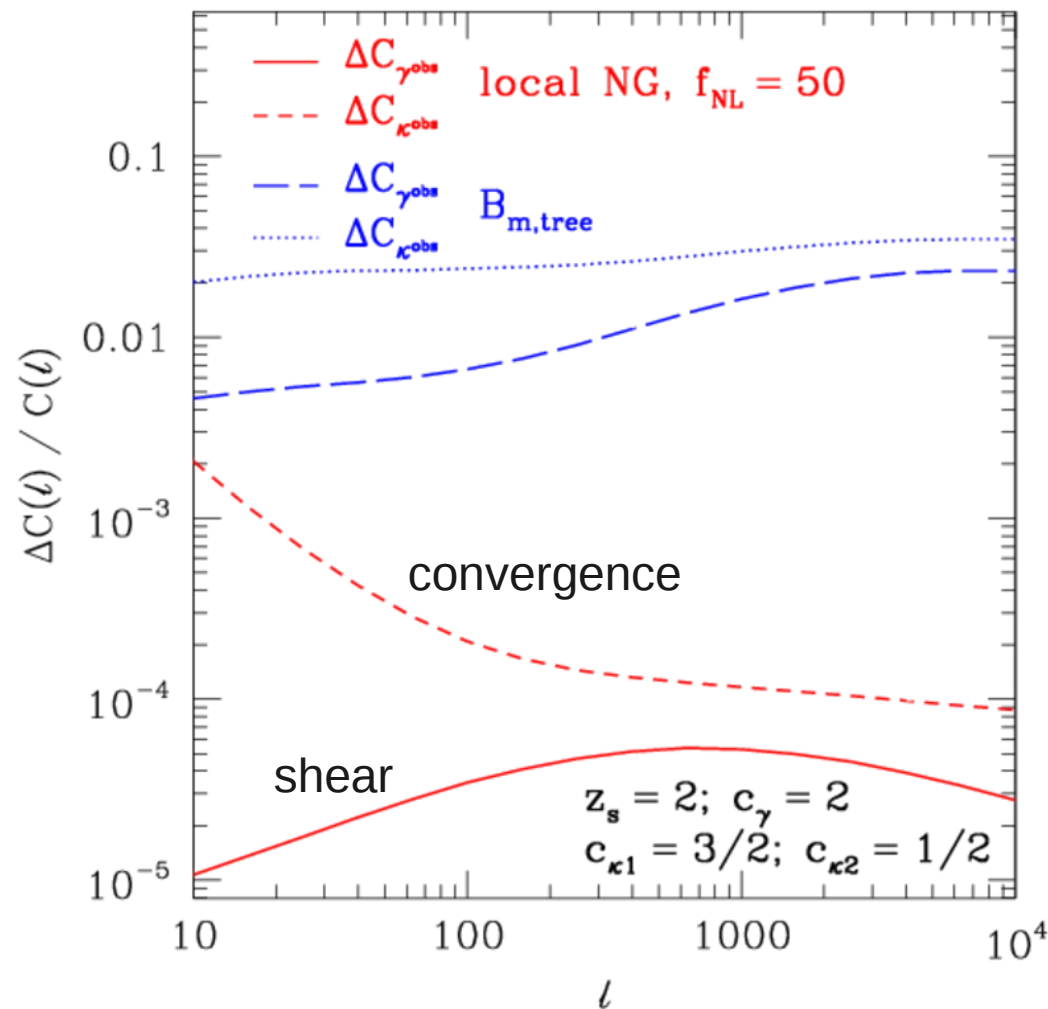
- Lensing power spectra receive contribution from primordial NG:

$$\Delta C^{\kappa\kappa}(\ell) \propto \int \frac{d^2 \ell_1}{(2\pi)^2} B_{\kappa}(\ell_1, |\vec{\ell} - \vec{\ell}_1|, \ell) \times (\text{geometric factors})$$

$\kappa$  bispectrum in squeezed limit  
- projection of matter bispectrum

# NG with Weak Lensing

- Unfortunately, effect is very small...



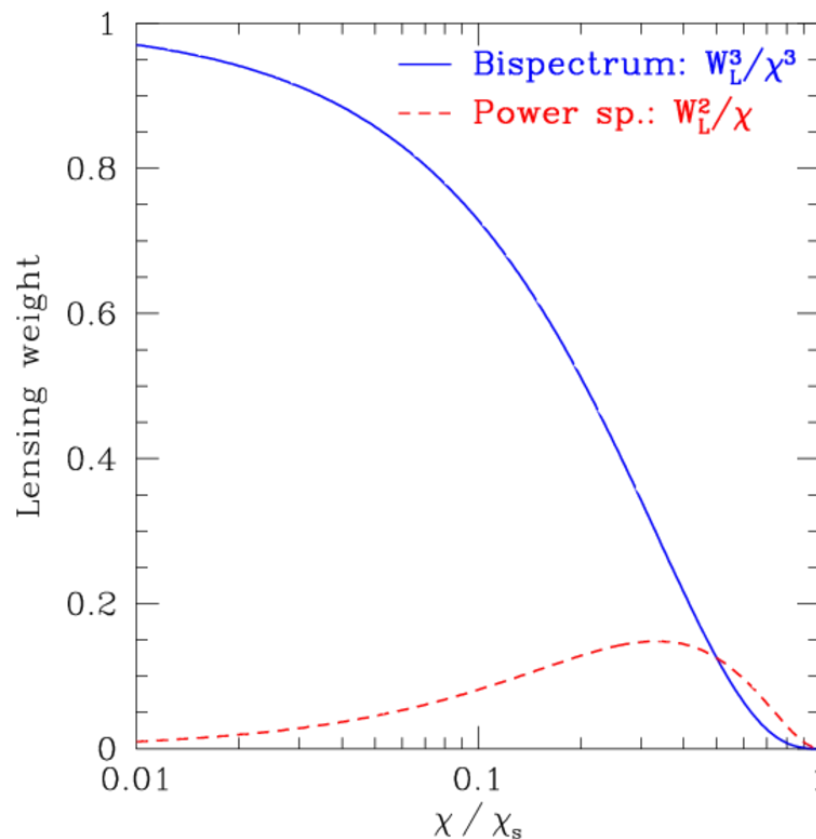
Relative magnitude of contributions to lensing power spectra

From tree-level bispectrum (gravitational collapse)

From local primordial NG

# NG with Weak Lensing

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# NG with Weak Lensing

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  - 1) Projection favors low redshifts  $\rightarrow$  small scales
  - 2) **Central limit theorem**: effect is suppressed by

$$L_p / \Delta\chi$$

$$\Delta\chi \sim \text{Gpc} \quad \text{width of projection kernel}$$

$$L_p \equiv \int \frac{d^2k}{(2\pi)^2} P(k) \approx 75 \text{ Mpc} \quad \text{1D coherence length of matter density field}$$

# NG with Weak Lensing

- Two very basic, generic reasons:
  - 1) Projection favors low redshifts → small scales
  - 2) **Central limit theorem**: effect is suppressed by

$$L_p / \Delta\chi$$

- These apply to *any non-linear tracer of any projected density field*
  - E.g. shear peaks, IR/UV backgrounds, ...

# Summary

- Galaxy clustering offers rich possibilities for testing inflation through non-Gaussianity
  - Scale-dependent bias: *non-trivial  $k$ - and  $M$ -dependence*
  - Complementary to CMB
  - NG halo bias on large scales now understood, including GR corrections
  - *More work needed for smaller scales...*
- On the other hand, *weak lensing* (in itself) is not a promising probe of NG